



St Helenas C of E Primary School

Power Maths White Rose Edition calculation policy and progression document, LOWER KS2



KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply. In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns.

By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively. Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single diait.

Children develop column methods to support multiplications in these cases.

For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount and develop this with the aid of a bar model and other representations alongside.

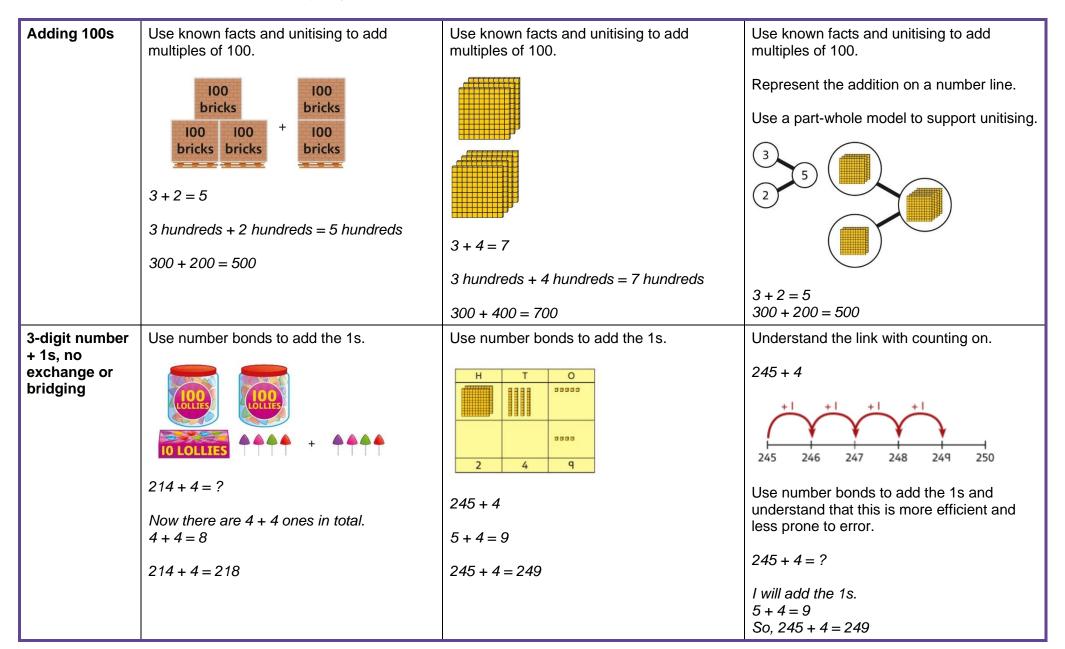
in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.



	Year 3			
	Concrete	Pictorial	Abstract	
Year 3 Addition				
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens. Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.010020030060070050040020000	
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use equipment to represent numbers to 1,000. 200 240 241 241 Use a place value grid to support the structure of numbers to 1,000. Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.	Represent the parts of numbers to 1,000 using a part-whole model. 215 200 10 $5215 = 200 + 10 + 5Recognise numbers to 1,000 representedon a number line, including those betweenintervals.$	

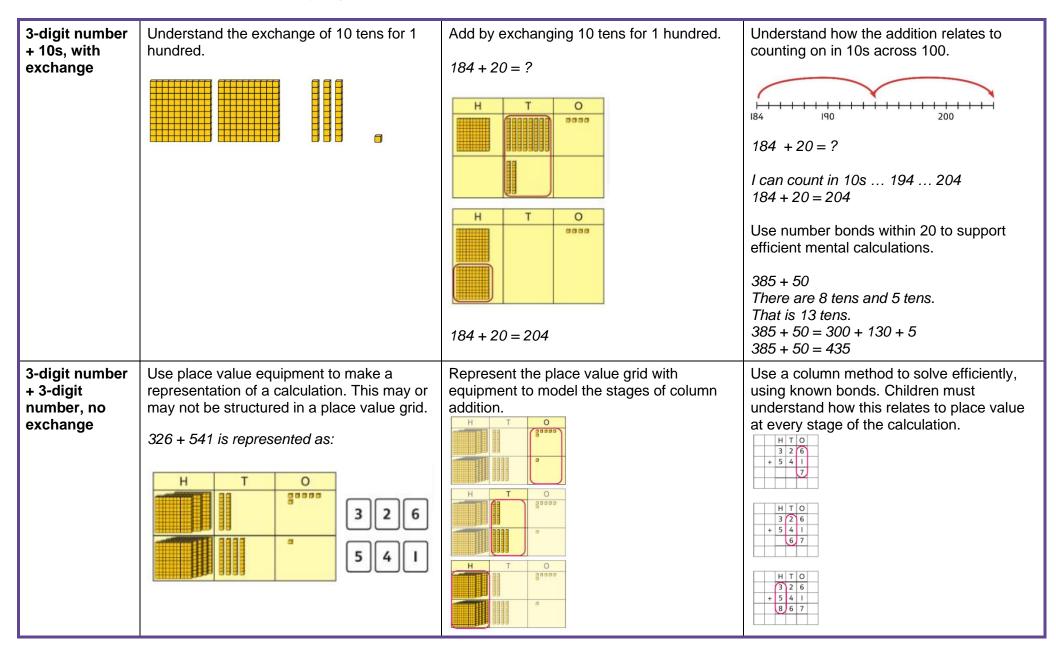




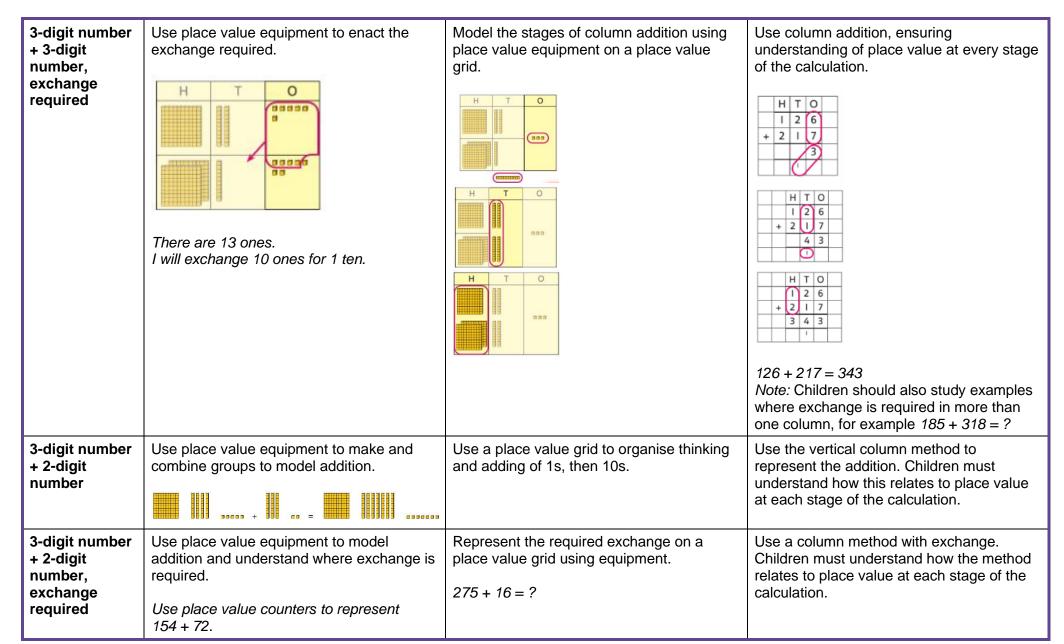


3-digit number + 10s, no exchange	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.
ege	234 + 50 There are 3 tens and 5 tens altogether. 3 + 5 = 8 In total there are 8 tens. 234 + 50 = 284	351 + 30 = ? $H T O$ $H T O$ $I O$	753 + 40 I know that 5 + 4 = 9 So, 50 + 40 = 90 753 + 40 = 793
3-digit number + 1s with exchange	Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten. Children should explore this using unitised objects or physical apparatus.	Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding. $\begin{array}{c} H \\ \hline \\$	Understand how to bridge by partitioning to the 1s to make the next 10. 7 5 2 $135 + 7 = ?$ $135 + 5 + 2 = 142Ensure that children understand how to add1s bridging a 100.198 + 5 = ?$ $198 + 2 + 3 = 203$









	Use this to decide if any exchange is required. There are 5 tens and 7 tens. That is 12 tens so I will exchange.	HTOHTOHTIII <t< th=""><th>$\begin{array}{c} \hline H T 0 \\ \hline 2 7 5 \\ + 1 6 \\ \hline 2 7 5 \\ + 1 6 \\ \hline 4 1 \\ \hline 2 7 5 \\ + 1 6 \\ - 1 6 \\ - 1$</th></t<>	$ \begin{array}{c} \hline H T 0 \\ \hline 2 7 5 \\ + 1 6 \\ \hline 2 7 5 \\ + 1 6 \\ \hline 4 1 \\ \hline 2 7 5 \\ + 1 6 \\ - 1 6 \\ - 1 $
Representing addition problems, and selecting appropriate methods	Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps. These representations will help them to select appropriate methods.	Children understand and create bar models to represent addition problems. 275 + 99 = ? 374 275 + 99 = 374	Use representations to support choices of appropriate methods.

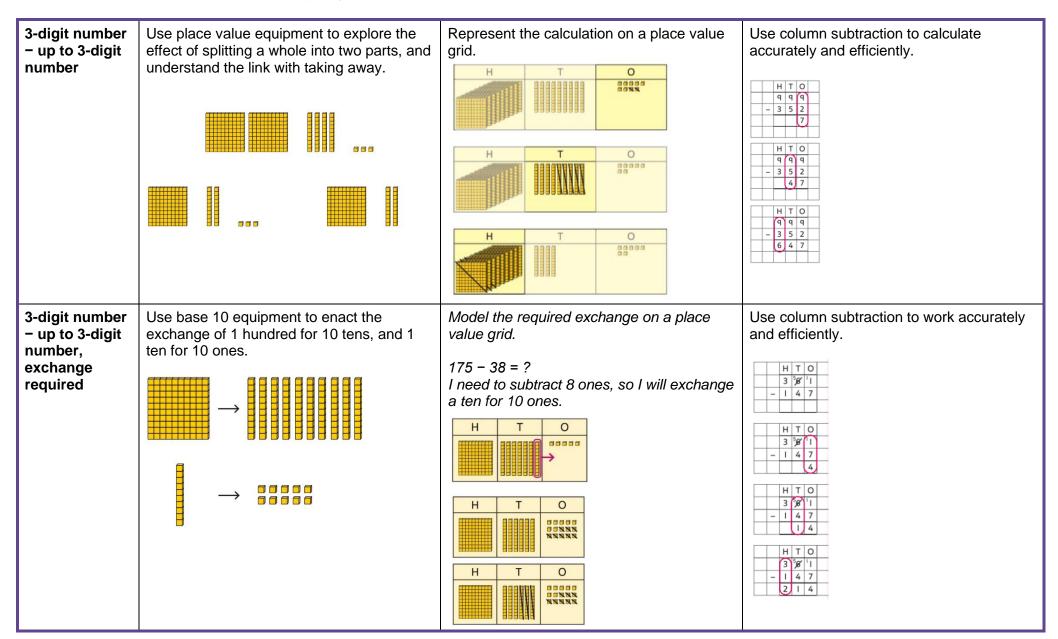
			128 + 105 + 83 = ? I need to add three numbers. $128 + 105 = 233$ 233 1 128 105 83 316 233 83
Year 3 Subtraction			
Subtracting 100s	Use known facts and unitising to subtract multiples of 100. 100 bricks bricks bricks bricks $5-2=3$ 500-200=300	Use known facts and unitising to subtract multiples of 100. 4 - 2 = 2 $400 - 200 = 200$	Understand the link with counting back in 100s. 100 100 200 300 400 $500400 - 200 = 200Use known facts and unitising as efficientand accurate methods.1$ know that $7 - 4 = 3$. Therefore, 1 know that 700 - 400 = 300.
3-digit number − 1s, no exchange	Use number bonds to subtract the 1s.	Use number bonds to subtract the 1s.	 Understand the link with counting back using a number line. Use known number bonds to calculate mentally. 476 - 4 = ?



	214 - 3 = ? IDENTIFY 4 - 3 = 1 $214 - 3 = 211$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	476 $400 70 6$ $6 - 4 = 2$ $476 - 4 = 472$
3-digit number – 1s, exchange or bridging required	Understand why an exchange is necessary by exploring why 1 ten must be exchanged. Use place value equipment.	Represent the required exchange on a place value grid. 151 - 7 = ? H T O H T O H T O KXXXX	Calculate mentally by using known bonds. 151 - 7 = ? 151 - 1 - 6 = 144

3-digit number − 10s, no exchange	Subtract the 10s using known bonds. 10 = 7 $381 - 10 = 7$	Subtract the 10s using known bonds. $\begin{array}{c c} H & T & O \\ \hline $	Use known bonds to subtract the 10s mentally. 372 - 50 = ? 70 - 50 = 20 So, 372 - 50 = 322
3-digit number	8 tens with 1 removed is 7 tens. 381 - 10 = 371 Use equipment to understand the exchange	Represent the exchange on a place value	Understand the link with counting back on a
- 10s, exchange or bridging required	of 1 hundred for 10 tens.	Represent the exchange of a place value grid using equipment. 210 - 20 = ? H T O I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.	Use flexible partitioning to support the calculation. 235 - 60 = ? 235 = 100 + 130 + 5
		H = 1 = 0 210 - 20 = 190	235 = 100 + 130 + 5 235 - 60 = 100 + 70 + 5 = 175

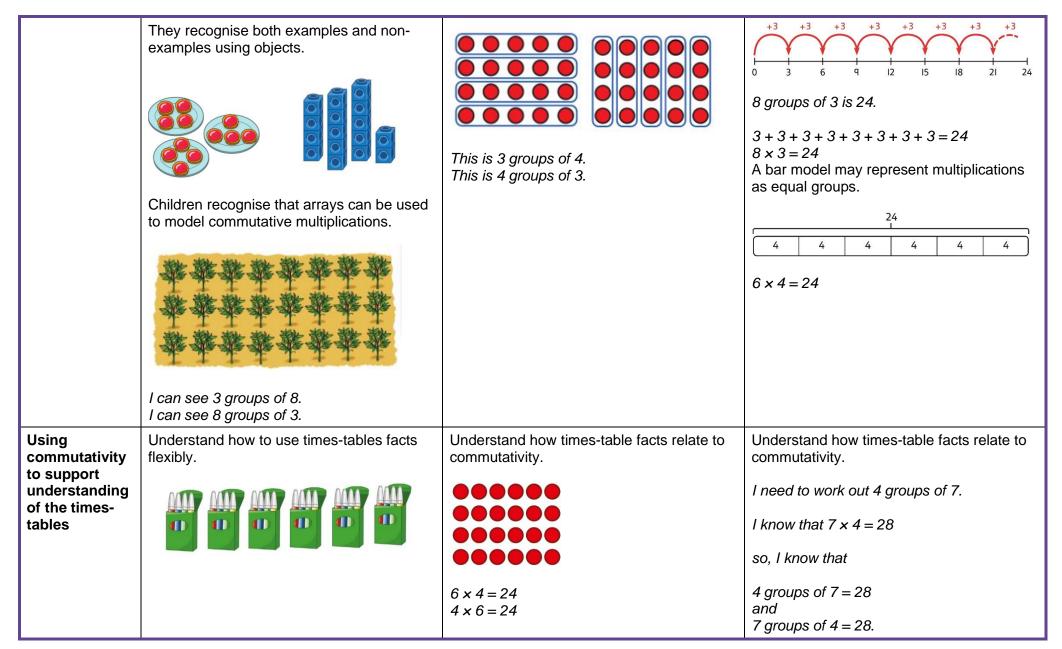






			If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly. Children should also understand how to exchange in calculations where there is a zero in the 10s column.
Representing subtraction problems		Use bar models to represent subtractions. 'Find the difference' is represented as two bars for comparison. Team A 454 Team B 128 ← ? Bar models can also be used to show that a part must be taken away from the whole.	Children use alternative representations to check calculations and choose efficient methods. Children use inverse operations to check additions and subtractions. The part-whole model supports understanding. <i>I have completed this subtraction.</i> 525 - 270 = 255 <i>I will check using addition.</i> 1 + 2 5 5 + 5 2 5 + 5 +
Year 3 Multiplication			
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition.	Children recognise that arrays demonstrate commutativity.	Children understand the link between repeated addition and multiplication.





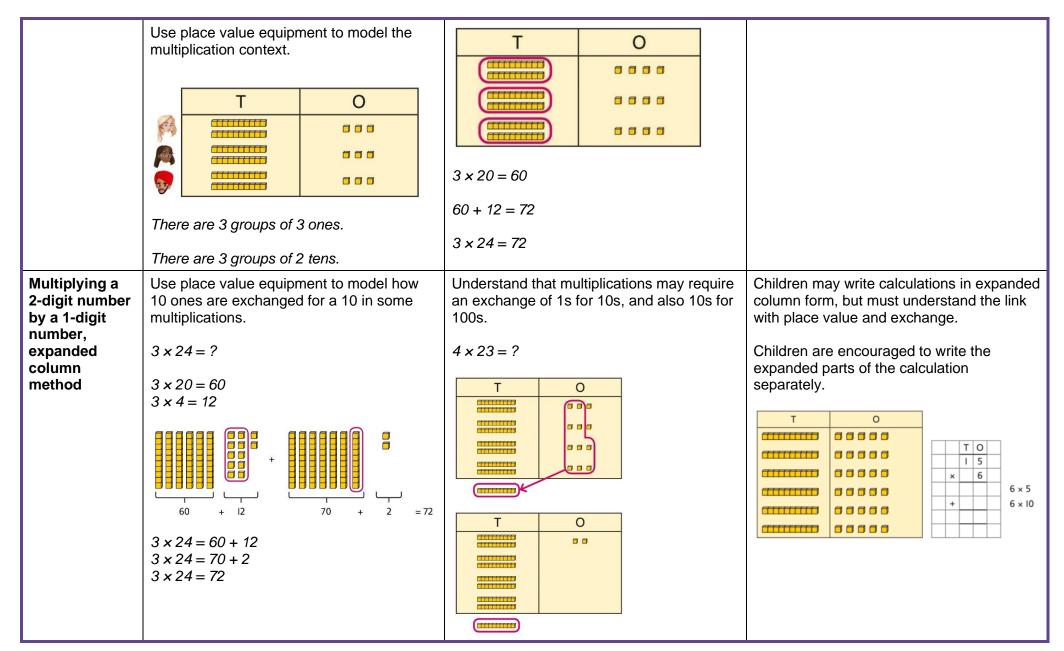


	There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls. I can use 6 × 4 = 24 to work out both totals.		
Understanding and using x3, x2, x4 and x8 tables.	Children learn the times-tables as 'groups of but apply their knowledge of commutativity. Image: Commutativity in the second s	Children understand how the x2, x4 and x8 tables are related through repeated doubling.	Children understand the relationship between related multiplication and division facts in known times-tables. $2 \times 5 = 10$ $5 \times 2 = 10$ $10 \div 5 = 2$ $10 \div 2 = 5$
Using known facts to multiply 10s, for example 3 × 40	Explore the relationship between known times-tables and multiples of 10 using place value equipment.	Understand how unitising 10s supports multiplying by multiples of 10.	Understand how to use known times-tables to multiply multiples of 10.



	Make 4 groups of 3 ones.		$\begin{array}{c} +2 & +2 & +2 & +2 \\ +2 & +2 & +2 & +2 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{array}$
	What is the same? What is different?	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} +20 +20 +20 +20 \\ 0 & 10 & 20 & 30 & 40 & 50 & 60 & 70 & 80 \end{array}$ $4 \times 2 = 8 \\ 4 \times 20 = 80 \end{array}$
Multiplying a 2-digit number by a 1-digit number	Understand how to link partitioning a 2-digit number with multiplying. Each person has 23 flowers. Each person has 2 tens and 3 ones. Each person has 2 tens and 3 ones. There are 3 groups of 2 tens. There are 3 groups of 3 ones.	Use place value to support how partitioning is linked with multiplying by a 2-digit number. $3 \times 24 = ?$	Use addition to complete multiplications of 2-digit numbers by a 1-digit number. $4 \times 13 = ?$ $4 \times 3 = 12$ $4 \times 10 = 40$ 12 + 40 = 52 $4 \times 13 = 52$







		$4 \times 23 = 92$ T 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	$23 \times 5 = ?$ $\begin{array}{r} H T O \\ 2 3 \\ \times 5 \\ 1 5 \\ + 1 0 0 \\ 1 1 5 \\ \hline \end{array} \qquad \qquad$
Year 3 Division			
Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions.	Use knowledge of known times-tables to calculate divisions.	Use knowledge of known times-tables to calculate divisions. <i>I need to work out 30 shared between 5.</i> <i>I know that</i> $6 \times 5 = 30$ <i>so I know that</i> $30 \div 5 = 6$. A bar model may represent the relationship between sharing and grouping. 24 4 4 4 4 4 4 4



		48 divided into groups of 4. There are 12 groups.	Children understand how division is related to both repeated subtraction and repeated addition.
		$4 \times 12 = 48$ $48 \div 4 = 12$	
			24 ÷ 8 = 3
			+8 $+8$ $+8$ $+8$ $+8$ $+8$ $+8$ $+8$
			$32 \div 8 = 4$
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.	Use images to explain remainders.	Understand that the remainder is what cannot be shared equally from a set.
		****	22 ÷ 5 = ?
	There are 13 sticks in total. There are 3 groups of 4, with 1 remainder.	22 ÷ 5 = 4 remainder 2	3 × 5 = 15 4 × 5 = 20 5 × 5 = 25 this is larger than 22 So, 22 ÷ 5 = 4 remainder 2
Using known facts to divide	Use place value equipment to understand how to divide by unitising.	Divide multiples of 10 by unitising.	Divide multiples of 10 by a single digit using known times-tables.
multiples of 10	Make 6 ones divided by 3.		180 ÷ 3 = ?
			180 is 18 tens.
	Now make 6 tens divided by 3.		18 divided by 3 is 6.



	What is the same? What is different?	12 tens shared into 3 equal groups. 4 tens in each group.	18 tens divided by 3 is 6 tens. 18 ÷ 3 = 6 180 ÷ 3 = 60
2-digit number divided by 1-digit number, no remainders	Children explore dividing 2-digit numbers by using place value equipment. $48 \div 2 = ?$ First divide the 10s. Then divide the 1s. 1000	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate. $ \begin{array}{r} 68\\60\\60\\8\end{array} $ $ \begin{array}{r} 60 \div 2 = 30\\8 \div 2 = 34\\68 \div 2 = 34\\\\68 \div 2 = $



2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder. Make 29 from place value equipment. Share it into 2 equal groups.	Use place value equipment to understand the concept of remainder in division. $29 \div 2 = ?$ $29 \div 2 = 14$ remainder 1	Partition to divide, understanding the remainder in context. 67 children try to make 5 equal lines. 67 = 50 + 17 $50 \div 5 = 10$ $17 \div 5 = 3$ remainder 2 $67 \div 5 = 13$ remainder 2 There are 13 children in each line and 2 children left out.
		Year 4	
	Concrete	Pictorial	Abstract
Year 4 Addition			
Understanding numbers to 10,000	Use place value equipment to understand the place value of 4-digit numbers.	Represent numbers using place value counters once children understand the relationship between 1,000s and 100s. (100) (10) (10) (10) (10) (10) (10) (10) (10)	Understand partitioning of 4-digit numbers, including numbers with digits of 0. 5,000 + 60 + 8 = 5,068 Understand and read 4-digit numbers on a number line.

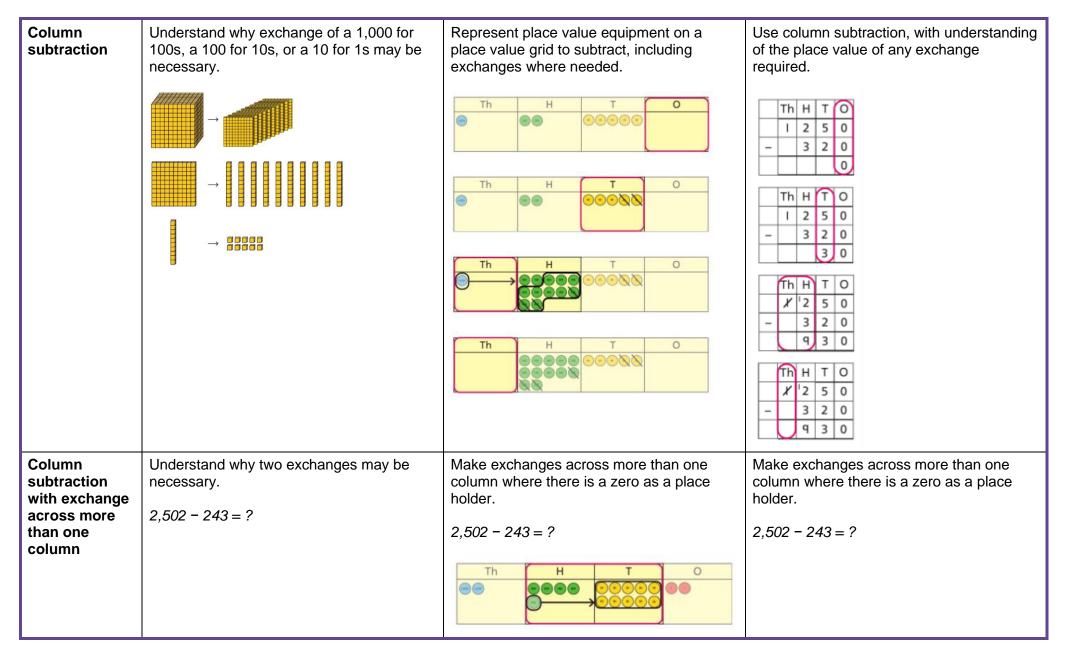


Choosing mental methods where appropriate	Use unitising and known facts to support mental calculations. <i>Make 1,405 from place value equipment.</i> <i>Add 2,000.</i> <i>Now add the 1,000s.</i> <i>1 thousand + 2 thousands = 3 thousands</i> <i>1,405 + 2,000 = 3,405</i>	Use unitising and known facts to support mental calculations. Th H T O O O O O O O O O O O O O O O O O O O	Use unitising and known facts to support mental calculations. 4,256 + 300 = ? 2 + 3 = 5 $200 + 300 = 5004,256 + 300 = 4,556$
Column addition	Use place value equipment on a place value grid to organise thinking. Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers. Use equipment.to show 1,905 + 775. Th H T 0 0 0 0 Why have only three columns been used for the second row? Why is the Thousands box empty? Which columns will total 10 or more?	Use place value equipment to model required exchanges.	Use a column method to add, including exchanges. Th H T O 1 5 5 4 + 4 2 3 7 5 7 9 1 Include examples that exchange in more than one column.



Representing additions and checking strategies		Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate. $\boxed{1,225}$ 799 574 $\boxed{\frac{1}{799}}$ $\boxed{\frac{1}{799}}$ $\boxed{\frac{1}{799}}$ $\boxed{\frac{1}{1373}}$ I chose to work out 574 + 800, then subtract 1. $\boxed{\frac{6,000}{1}}$ $\boxed{2,999}$ $\boxed{3,001}$ This is equivalent to 3,000 + 3,000.	Use rounding and estimating on a number line to check the reasonableness of an addition. $1 \rightarrow 1,000\ 2,000\ 3,000\ 4,000\ 5,000\ 6,000\ 7,000\ 8,000\ 9,000\ 10,000$ 912 + 6,149 = ? I used rounding to work out that the answer should be approximately 1,000 + 6,000 = 7,000.
Year 4			
Subtraction Choosing	Use place value equipment to justify mental	Use place value grids to support mental	Use knowledge of place value and unitising
mental methods	methods.	methods where appropriate.	to subtract mentally where appropriate.
where appropriate		Th H T O Image:	3,501 - 2,000
			3 thousands – 2 thousands = 1 thousand
		7,646 - 40 = 7,606	3,501 - 2,000 = 1,501
	What number will be left if we take away 300?		





	$ \begin{array}{c} \hline \\ \hline \\ \\ \hline \\ \hline \\ \\ \hline \\ \hline \\ \hline \\ \hline \\ \\ \hline \hline \\ \hline \\ \hline \hline \\ \hline \\ \hline \\ \hline \hline \\ \hline \\ \hline \hline \\ \hline \\ \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \hline \\ \hline \hline$	Th H T O	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Representing subtractions and checking strategies		Use bar models to represent subtractions where a part needs to be calculated. Total 5,762 2,899 Yes votes <i>I can work out the total number of Yes votes</i> <i>using 5,762 – 2,899</i> . Bar models can also represent 'find the difference' as a subtraction problem. Danny 899 Luis 1,005	Use inverse operations to check subtractions. I calculated 1,225 – 799 = 574. I will check by adding the parts. $\boxed{1,225} \\ \hline 799 \\ 574 \\ \hline Th H T O \\ \hline 1 3 7 4 \\ \hline 1 3 7 3 \\ \hline 1 1 1 $



Year 4 Multiplication			
Multiplying by multiples of 10 and 100	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100. 3 groups of 4 ones is 12 ones. 3 groups of 4 tens is 12 tens. 3 groups of 4 hundreds is 12 hundreds.	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100. $3 \times 4 = 12$ $3 \times 40 = 120$ $3 \times 400 = 1,200$	Use known facts and understanding of place value and commutativity to multiply mentally. $4 \times 7 = 28$ $4 \times 70 = 280$ $40 \times 7 = 280$ $4 \times 700 = 2,800$ $400 \times 7 = 2,800$
Understanding times-tables up to 12 x 12	Understand the special cases of multiplying by 1 and 0. $5 \times 1 = 5$ $5 \times 0 = 0$	Represent the relationship between the x9 table and the x10 table. Represent the x11 table and x12 tables in relation to the x10 table. $2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 12 = 40 + 8$	Understand how times-tables relate to counting patterns. Understand links between the x3 table, x6 table and x9 table 5×6 is double 5×3 x5 table and x6 table <i>I know that</i> $7 \times 5 = 35$ so <i>I know that</i> $7 \times 6 = 35 + 7$. x5 table and x7 table $3 \times 7 = 3 \times 5 + 3 \times 2$ 3×5 3×7 x9 table and x10 table $6 \times 10 = 60$ $6 \times 9 = 60 - 6$



Understanding and using partitioning in multiplication	Make multiplications by partitioning. 4×12 is 4 groups of 10 and 4 groups of 2. $4 \times 12 = 40 + 8$	Understand how multiplication and partitioning are related through addition. Understand how multiplication and partitioning are related through addition. Understand how multiplication and $4 \times 3 = 12$ $4 \times 3 = 12$ $4 \times 3 = 12$ $4 \times 5 = 20$ 12 + 20 = 32 $4 \times 8 = 32$	Use partitioning to multiply 2-digit numbers by a single digit. $18 \times 6 = ?$ $18 \times 6 = ?$ $18 \times 6 = ?$ $18 \times 6 = 10 \times 6 + 8 \times 6$ $= 60 + 48$ $= 108$ $18 \times 6 = 10 \times 6 + 8 \times 6$ $= 60 + 48$ $= 108$
Column multiplication for 2- and 3-digit numbers multiplied by a single digit	Use place value equipment to make multiplications. Make 4×136 using equipment. Make 4×136 using equipment. Make 4×136 using equipment. I can work out how many 1s, 10s and 100s. There are 4×6 ones 24 ones There are 4×3 tens 12 tens There are 4×1 hundreds 4 hundreds 24 + 120 + 400 = 544	Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.	Use the formal column method for up to 3-digit numbers multiplied by a single digit. $\begin{array}{r} H T O \\\hline 3 1 2 \\\hline \times 3 \\\hline 9 3 6 \\\hline \end{array}$ Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation.

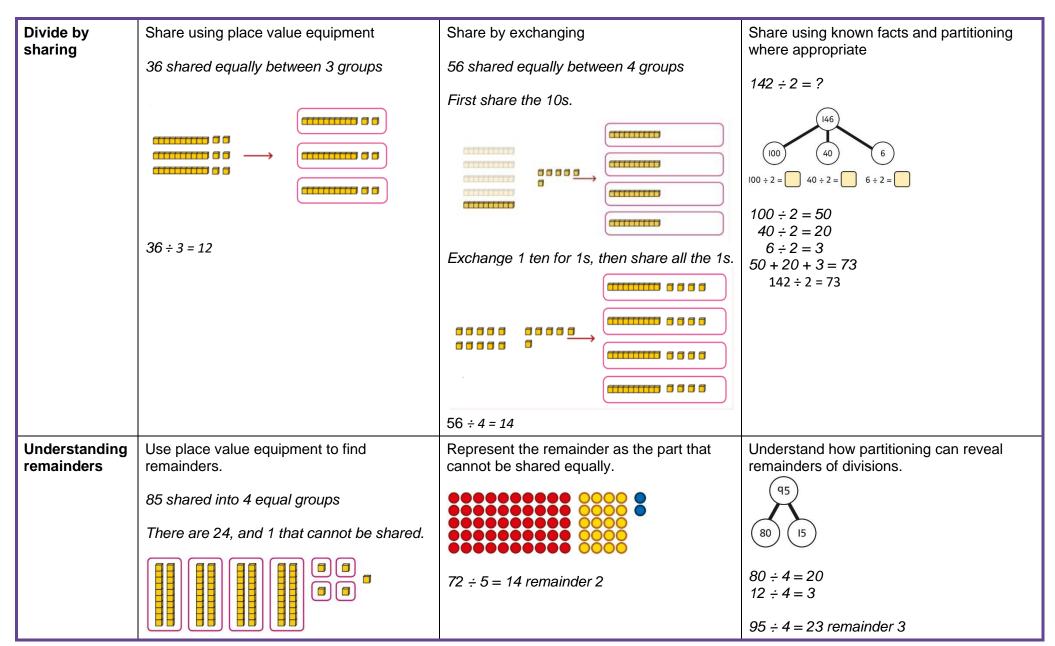


			H T O 2 3 × 5 - 1 + 1 0 0 × 5 + 1 1 1 5 1 1 1 5 1 1 1 5 1 1 5 1 1
Multiplying more than two numbers	Represent situations by multiplying three numbers together.	Understand that commutativity can be used to multiply in different orders. 000000000000000000000000000000000000	Use knowledge of factors to simplify some multiplications. $24 \times 5 = 12 \times 2 \times 5$ $12 \times 2 \times 5 =$ $12 \times 10 = 120$ So, $24 \times 5 = 120$
Year 4 Division			
Understanding the relationship between multiplication and division, including times-tables	Use objects to explore families of multiplication and division facts.	Represent divisions using an array.	Understand families of related multiplication and division facts. <i>I know that</i> $5 \times 7 = 35$ <i>so I know all these facts:</i>



	4 × 6 = 24 24 is 6 groups of 4. 24 is 4 groups of 6. 24 divided by 6 is 4. 24 divided by 4 is 6.	28 ÷ 7 = 4	$5 \times 7 = 35$ $7 \times 5 = 35$ $35 = 5 \times 7$ $35 = 7 \times 5$ $35 \div 5 = 7$ $35 \div 7 = 5$ $7 = 35 \div 5$ $5 = 35 \div 7$
Dividing multiples of 10 and 100 by a single digit	Use place value equipment to understand how to use unitising to divide.	Represent divisions using place value equipment. $q_{\pm 3} =$ $q_{\pm 3} =$ $q_{\pm 3} =$ $q_{0 \pm 3} =$ $q_{0 $	Use known facts to divide 10s and 100s by a single digit. $15 \div 3 = 5$ $150 \div 3 = 50$ $1500 \div 3 = 500$





Power Maths White Rose Edition calculation policy

